



The Efficiency of Noble Gas Trapping in Astrophysical Environments

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Abstract

Amorphous ice has long been invoked as a means for trapping extreme volatiles into solids, explaining the abundances of these species in comets and planetary atmospheres. Experiments have shown that this trapping is possible and has been used to estimate the abundances of each species in primitive ices after they have formed. However, these experiments have been carried out at deposition rates that exceed those expected in a molecular cloud or solar nebula by many orders of magnitude. Here, we develop a numerical model that reproduces the experimental results and apply it to those conditions expected in molecular clouds and protoplanetary disks. We find that two regimes of ice trapping exist: *burial trapping*, where the ratio of trapped species to water in the ice reflects that same ratio in the gas; and *equilibrium trapping*, where the ratio in the ice depends only on the partial pressure of the trapped species in the gas. The boundary between these two regimes is set by both the temperature and rate of ice deposition. These effects must be accounted for when determining the source of trapped volatiles during planet formation.

Key words: astrochemistry – comets: general – ISM: general – planets and satellites: atmospheres – protoplanetary disks

1. Introduction

The incorporation of noble gases into early planetesimals is of interest for many reasons. The Galileo spacecraft found that the abundances of these elements relative to hydrogen, along with other volatile elements such as C and N, were elevated in Jupiter when compared to the solar nebula, suggesting that the giant planet's atmosphere was polluted by planetesimals with solar abundances of all elements, except for H and He (Owen et al. 1999). The presence of noble gases in terrestrial planet atmospheres has been suggested to have arisen, at least in part, due to accretion of comets over their histories (e.g., Dauphas 2003; Notesco et al. 2003; Notesco & Bar-Nun 2005; Marty et al. 2017). This idea is supported by recent observations from the *Rosetta* mission, which indicate that noble gases (Ar) are indeed present within the comet and which show that solid bodies did incorporate some amount of noble gases (Balsiger et al. 2015).

How these elements were incorporated into primitive bodies remains a mystery. Noble gases have very low condensation temperatures (<50 K Gautier et al. 2001; Lodders 2003), suggesting that these elements would not be contained within the solids present where planets formed. Water could serve as a carrier for these elements, trapping them within an icy matrix so that they would only be lost once higher temperatures were reached. However, how the water ice could incorporate the noble gases into its structure is still debated, with two primary methods currently being discussed. In explaining Jupiter's atmospheric composition, Owen et al. (1999) proposed that the elements were trapped as amorphous water ice formed on solids, with guest species being surrounded and buried by water molecules freezing-out in cold environments. This trapping has been seen experimentally at very low temperatures (<50 K, e.g., Bar-Nun et al. 1985, 1988), implying that Jupiter accreted solids that formed at the very distant edges of the solar system. Gautier et al. (2001) instead suggested that the noble gases were incorporated within crystalline water ice as

clathrates, which were predicted to form at higher temperatures than the vaporization point of the guest molecules (Lunine & Stevenson 1985; Mousis et al. 2016).

Amorphous ice and clathrates form under very different temperature and pressure conditions, thus identifying which form of ice the noble gases were originally locked away in. This will provide important insights into the history of water during the early stages of planet formation. However, if we wish to determine which of these forms was the dominant carrier for the noble gases (as well as other volatiles such as CO and N₂), then we must understand the efficiency with which gases are incorporated into ice in the various environments that existed during the birth of our solar system. Here, we focus on the issue of trapping in amorphous ice. While experimental studies have been used to estimate the conditions under which primitive ices may have formed (e.g., Notesco & Bar-Nun 2005), these experiments and those of others (e.g., Collings et al. 2003; Fayolle et al. 2011; Yokochi et al. 2012), were performed at very high deposition rates of water ice, which would imply freeze-out fluxes that are many orders of magnitude above those expected in astrophysical environments. These experimental conditions are necessary to study the processes at work on laboratory timescales; however, it is unclear how these results can be extrapolated to the very different conditions that are expected during planet formation.

In this paper, we develop a mathematical model to understand how noble gases would be locked away in amorphous ices that formed in the ISM or outer solar nebula. In the next section, we review the experimental work that has been done on noble gas trapping. We then describe the three-phase model that is used to quantitatively investigate how water and guest species are exchanged between the gas, solid surface, and mantle of amorphous ice, while fitting the model parameters to reproduce the experimental results and trends described by previous studies. We then apply these models to various astrophysical environments to evaluate the efficiency of this process. In interpreting these results, we consider what

physical processes must be considered in future work, both theoretical and experimental, to evaluate the role that amorphous ice trapping played in setting the noble gas inventories of planetary bodies.

2. Review of Noble Gas Trapping Experiments

The trapping of volatile species by water ice has been studied by a number of authors using a variety of experimental setups (e.g., Bar-Nun et al. 1988; Sandford & Allamandola 1990; Collings et al. 2003; Fayolle et al. 2011; Yokochi et al. 2012). We focused on the studies by Bar-Nun and collaborators (e.g., Bar-Nun et al. 1988; Notesco et al. 1999, 2003; Notesco & Bar-Nun 2005) in developing our numerical model because they have reported the largest collection of experimental results, and thus provide a set of numbers from a wide range of conditions that can be used to constrain the key parameters in our model. Furthermore, it was these results that motivated Owen et al. (1999) to suggest that Jupiter's atmospheric composition may be explained by trapping in this manner. Here, we explain the conceptual framework for those experiments and return to the results of other studies in our later discussions.

In the experiments, a mix of water vapor and a guest species (here we focus on Ar as a representative noble gas/volatile) flowed over a cold plate within an experimental chamber via cryopumping. The cold plate was set at a given temperature and the rate of flow was controlled (remained constant) so that layers of ice measuring $\sim 0.1 \mu\text{m}$ thick were deposited on timescales of minutes to days (deposition rates of ice of 10^{-5} – $10^{-1} \mu\text{m minute}^{-1}$). After deposition, the experimental chamber was then pumped down to remove any remaining gas and the cold plate was heated at rates of ~ 1 – 10 K minute^{-1} . During heating, gas was continuously pumped away and its composition was measured. The composition was assumed to reflect what was sublimated from the ice at that time or temperature.

While Ar was found to be present in the chamber throughout the experiment, its abundance increased rapidly at particular instances during warming. Immediately after heating began, the flux of Ar into the pump rose significantly above the background. This was interpreted as some amount of frozen Ar that came from the deposited solid. That is, this Ar was not physically trapped within the ice but was adsorbed onto the substrate and thus was liberated to the gas phase due to direct thermal desorption. The second, significant pulse of Ar came when temperatures reached $\sim 120 \text{ K}$, when water molecules also began to desorb. Because this Ar was only released once water itself also began to be seen in the vapor, this was interpreted as Ar that was trapped within the amorphous ice-atoms that were unable to desorb due to a physical barrier provided by the water molecules.

Again, Ar was found in the gas throughout the experiments. Beyond vaporization, the amorphous water ice also would evolve physically because molecules within the ice would diffuse or rearrange themselves when undergoing various phase transitions at temperatures $> 80 \text{ K}$. Release of vapor could occur as these physical changes take place, which has been reported in other experimental studies (Collings et al. 2003; Viti et al. 2004). The total amount of Ar trapped in the Bar-Nun group's experiments was defined by that released after the first pulse of Ar had declined to background levels, which occurred

once warming brought the sample to $T \sim 50 \text{ K}$ (Notesco et al. 2003; Notesco & Bar-Nun 2005).

A few critical assumptions are made in interpreting the measurements from this study that are important to highlight. The first is that all freezing-out and desorption of water and Ar occurred on the cold plate and nowhere else in the experimental chamber. If materials were frozen out elsewhere, then it is possible that the Ar that is measured was not trapped but instead originated from an unrelated region in the experimental chamber. This would be particularly important because the cold plate was warmed in the experiments and not the entire chamber. If temperature gradients were present, then it is possible that Ar that was frozen-out (not trapped) desorbed while the cold plate was at a higher temperature than the region where the Ar was actually released. Finally, Ar was present throughout the warm-up phase, therefore it is possible that the gas that was pumped out was not an immediate reflection of what was desorbed from the ice, meaning that the recorded compositions were influenced by what was vaporized at a lower temperature than when the data was recorded. These issues were minimized by carrying out the experiments under high vacuum conditions and line-of-sight methods were used to maximize the measured desorption to a specific sample region. Nonetheless, these possibilities mean that the numbers from the experiments should be taken as upper limits on the amount of trapped Ar in the ice. Here, we follow the authors by assuming that the measurements reflect the actual ice composition, but return to this issue in the discussion.

3. Overview of the Three-phase Model

To understand how the composition of the ice evolved over time in these experiments, we adopt the basic three-phase model of Hasegawa & Herbst (1993). This model tracks the exchange of species between the gas and solid phases, with the solid phase divided into the surface, which communicates with the gas, and the mantle, which does not. We also extend the model by following Fayolle et al. (2011), who established a means to allow for the exchange of species between the mantle and the surface.

Exchange between the solid phase and gas phase occurs through adsorption and desorption of the various species considered. Adsorption occurs when a gaseous species collides with a solid substrate and sticks. Meanwhile, desorption occurs when a molecule at the surface leaves the solid surface and returns to the gas because the thermal energy it attains in the solid is enough to overcome its binding energy to the substrate. The mantle is formed when molecules or atoms freeze-out on top of already adsorbed species, burying them. An atom or molecule is added to the surface from the mantle when it is exposed by desorption of an overlying species, or through diffusion (swapping positions with other species).

The rate of adsorption by a gaseous species, and thus increase in the abundance of the surface species (per unit volume), n_i^s , is given by:

$$\frac{dn_i^s}{dt} = v_{\text{th}}^i n_i^g \quad (1)$$

where n_i^g is the number density of the molecule or atom in the gas, v_{th}^i is the thermal velocity of the gaseous species given by $v_{\text{th}}^i = \left(\frac{8kT}{\pi m_i}\right)^{\frac{1}{2}}$, and we have assumed every collision of the gas molecule onto the surface leads to sticking. Here, the surface

abundance is given by the number of molecules or atoms on the surface, N_s^i , times the number density of surfaces (dust grains in the astrophysical setting), n_d ; that is $n_i^s = N_s^i n_d$.

The rate of desorption of a species from the surface to the gas is given by the Polanyi–Wigner Equation, which describes the thermal desorption of solid species from a substrate as it is warmed (e.g., Bergin 2011; Smith et al. 2016; Chaabouni et al. 2018):

$$\frac{dn_i^s}{dt} = -\nu_i \exp\left(-\frac{E_i}{T_{\text{dust}}}\right) n_i^s \quad (2)$$

where n_i^s is the abundance of the molecule or atom at the surface of the solid, E_i is the binding energy (in units of K as we take $E_i = E_{\text{bind},i}/k$), and ν is the vibrational frequency of the species in the potential well, which keeps it bound to the surface and is of order $\nu \sim 10^{12} \text{ s}^{-1}$ for the species of interest here (Biham et al. 2001; Bergin 2011; Fayolle et al. 2011). While a single value for the binding energy is used here, the ice surface is likely to be heterogeneous, leading to a distribution of binding energies for a given species to the ice, as demonstrated for CO binding to water ice (e.g., Karssemeijer et al. 2014). The single value that is used here should be considered the most probable binding energy of the whole distribution of binding energies (Smith et al. 2016).

The mantle forms when adsorbing species land on top of already adsorbed species. Because the landing point of adsorbed molecules is random, the growth of the mantle during deposition is given by:

$$\frac{dn_i^m}{dt} = \alpha \frac{dn_s}{dt} \frac{n_i^s}{n_s} \quad (3)$$

where n_i^m is the abundance of the species in the mantle with $n_i^m = N_m^i n_d$. Here $\frac{dn_s}{dt}$ is the total sum of adsorption rates minus the rates of desorption for all species considered, α is the fraction of surface sites occupied at the time of adsorption. That is, a typical surface can host $\sim 10^{15}$ sites cm^{-2} . If only a portion of these sites are occupied, then an adsorbing species can either land on an already adsorbed species, moving that adsorbed species to the mantle, or it can fill a vacant surface site, thus not affecting the mantle at all. Thus, α represents the probability of landing on an occupied surface site, while $(1-\alpha)$ represents the probability that an adsorbing species landed on bare substrate instead of a previously adsorbed molecule or atom. Note that the surface may represent multiple partially filled monolayers of adsorbed particles—it represents the collection of species that are directly exposed to the gas (see Figure 1).

When the total desorption rates are greater than the total adsorption rates, then the mantle composition evolves as surface species are removed, which exposes buried species. These exposed species now become part of the surface and are no longer considered part of the mantle. In this case, the exchange between the surface and mantle is given by:

$$\frac{dn_i^s}{dt} = \left[\sum_j \nu e^{-\frac{E_j}{T}} n_j^s \right] \frac{n_i^m}{\sum_j n_j^m}. \quad (4)$$

In the absence of any other processes, a guest atom or molecule would become trapped once another species adsorbs

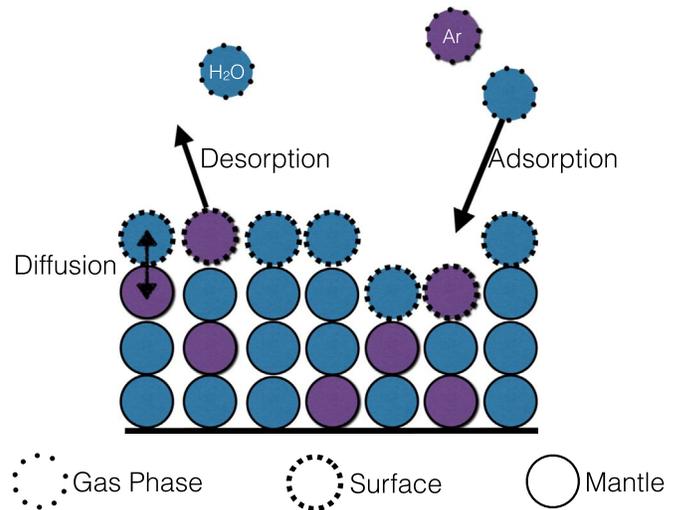


Figure 1. Schematic diagram of the three-phase model described here. We focus on the deposition and evolution of an H₂O-Ar mixture, where each species either exists in the gaseous, surface, or mantle phases. Evolution among these phases occurs through adsorption, desorption, and diffusion. This model is based on that developed and described by Fayolle et al. (2011).

above it. Release of the trapped species could only occur once all of the species that were adsorbed on top of it were desorbed. However, experiments have shown that volatiles incorporated into the mantles of deposited ice can also be lost, which suggests that swapping of species or exchange between the mantle and surface can occur (e.g., Öberg et al. 2009a; Fayolle et al. 2011). This was seen as greater amounts of the volatiles were lost from the ice at their respective desorption temperatures than could be explained from those present on the surface layer alone. This indicates that some fraction of the volatiles in the ice are trapped because they are only lost along with the binding water molecules, while others remain mobile and make their way to desorb directly at much lower temperatures.

The details of how migration of the volatile through the ice occurs remain uncertain—some of it possibly occurs within pores and cracks in the ice. However, trapping, and thus limitations on migration, is independent of the pores and cracks that are available because species with different volatilities (binding energies) such as CO and CO₂ are released from ice at very different temperatures, which cannot be explained simply by the physical restructuring or evolution of these pores and cracks (Fayolle et al. 2011).

In experimental studies, certain trends and relations were observed that must be reproduced in terms of the loss of a non-trapped component of the volatile. For example, it was found that the fraction of a trapped CO and CO₂ increased with increasing ice thickness (Fayolle et al. 2011). This is consistent with the findings of Notesco & Bar-Nun (2005), who found that higher trapped Ar/H₂O ratios were found in ice layers 5 μm thick when compared to those 0.1 μm thick. These experiments also showed that the fraction of the deposited volatile that was trapped increased as its relative abundance in the ice decreased. In other words, for the same amount of water, higher amounts of the trapped volatile led to greater fractions being lost during heating instead of trapped.

To account for the loss of volatiles in a manner that is consistent with the experimental behaviors described above, Fayolle et al. (2011) extended the three-phase model by

allowing molecules or atoms in the mantle to migrate to the surface. This model efficiently reproduced the desorption of species from a deposited $\text{CO}_2+\text{H}_2\text{O}$ and $\text{CO}+\text{H}_2\text{O}$ mixtures. The rate of exchange between the ice surface and mantle is given by:

$$R_i^{\text{diff}} = \frac{f_i \nu}{\sum_j n_j^m} e^{-\frac{E_{\text{diff}}}{T}} [n_{\text{H}_2\text{O}}^s n_i^m - n_i^s n_{\text{H}_2\text{O}}^m]. \quad (5)$$

Here E_{diff} is the energy of diffusion required for the species to swap locations with a surface water molecule. This energy can be related to the binding energy of species of interest. For simplicity, we follow Garrod (2013) by assuming they are proportional and set the value for $E_{\text{diff}} = 0.5E_i$. Later on, we will discuss how various values of E_{diff} would affect the results of this study.

In this equation, f_i represents the fraction of the non-water mantle that is able to migrate to the surface of the ice. That is, experiments suggest that only a portion of the mantle communicates with the surface to allow for migration of the volatile guest and that this varies with the relative abundance of that volatile contained within the mantle during deposition. Based on the experimental studies of Öberg et al. (2009a), the form of f_i is given by:

$$f_i = 1 - \frac{n_i^{m,\text{ini}} - c_i(x_i^{\text{ini}})^{\beta}}{n_i^m} \quad (6)$$

where $n_i^{m,\text{ini}}$ represents the initial abundance of the species of interest in the mantle after deposition and before heating and x_i^{ini} is the initial mixing ratio of the species to water in the mantle, $x_i = n_i^{m,\text{ini}}/n_{\text{H}_2\text{O}}^{\text{ini}}$. The parameter, c_i , is the availability constant and it describes the extent to which the mantle communicates with the surface. That is, given that f_i defines the fraction of the mantle species able to diffuse to the surface and be desorbed upon heating, $(1-f_i)$ is the fraction that remains trapped within the water ice. Thus, by knowing c_i , one can predict the amount of trapped guest molecules to remain in the ice:

$$n_i^{\text{tr}} = n_i^{m,\text{ini}} - c_i(x_i^{\text{ini}})^{\beta} \quad (7)$$

where we look at the instant immediately after deposition when $n_i^m = n_i^{m,\text{ini}}$. Upon heating, the $c_i(x_i^{\text{ini}})^{\beta}$ species will migrate to the surface of the ice and desorb as part of the frozen out species released initially upon warming, as seen in the experiments described above. The fraction of volatile that is trapped is given by:

$$f_i^{\text{tr}} = 1 - \frac{c_i}{n_{\text{H}_2\text{O}}^{\text{ini}}} x_i^{\beta-1}. \quad (8)$$

Thus, provided $\beta > 1$, as x_i decreases, the fraction of the original volatile that is trapped increases, which is in agreement with experiments (Öberg et al. 2009a; Fayolle et al. 2011). Furthermore, for the same conditions, as the ice gets thicker (as $n_{\text{H}_2\text{O}}^{\text{ini}}$ increases), the fraction of trapped volatile also increases; this is again in line with experimental results described above. Following Öberg et al. (2009a), we take $\beta = 2$, but have also explored other values (1–5) and found that they have little effect on our conclusions. Furthermore, we do not have to worry if the availability constant varies with ice

thickness because we only consider ice layers that are $0.1 \mu\text{m}$ thick, which enables us to be consistent with the experiments to which we are fitting model parameters.

The purpose of the availability constant is to set how the deposited volatile is distributed between the trapped component and the component the frozen component. Therefore, it is a measure of how mobile a given species is. Note that if $c_i = 0$, then all of the species in the mantle are trapped because no migration would occur. As c_i increases, the amount of trapped material decreases as more and more of the guest species is able to migrate from the mantle to the surface. In addition, Equation (8) predicts that the trapped fraction decreases as x_i (i.e., the ratio of the volatile to water in the deposited ice) increases. Furthermore, for higher values of $n_{\text{H}_2\text{O}}^{\text{ini}}$, or thicker ices, the fraction of trapped volatile increases. Consequently, this captures the behavior of the major effects observed in the experimental results described above.

Because water is expected to be much more abundant than argon in the solar nebula and molecular clouds, the details of diffusion and migration of untrapped species is likely to be unimportant, unless only portions of the water budget are in the vapor phase, which results in high $\text{Ar}/\text{H}_2\text{O}$ ratios in the gas. We will return to this point in the Summary and Discussion section.

While this approach is general enough for any species of interest, in the following application of the model, we continue to focus on Ar as a representative noble gas or volatile that could be trapped by the ice. The only unknowns in this model are the binding energy of Ar to the substrate, E_{Ar} , and the availability constant, c_{Ar} . Consequently, we vary these parameters to determine which provides the best match to the experimental results.

4. Modeling Experimental Results

To fit the parameters in our model to produce the results reported by Natesco et al. (2003), Natesco & Bar-Nun (2005), the experimental conditions must be translated to variables to be used in the equations given previously. We divide the experiment into two parts: deposition and warming. Deposition corresponds to the time when water and Ar are injected into the experimental chamber and freeze-out onto the gold-coated copper plate that, as reported by Bar-Nun et al. (1987), measured $5 \text{ cm} \times 2.5 \text{ cm}$ for a total 12.5 cm^2 in area. As a test in those experiments, a $2 \mu\text{m}$ thick layer of ice developed, which was estimated to correspond to 10^{19} – 10^{20} H_2O molecules. Assuming uniform thickness of the ice across the copper plate, and that species were only deposited on the plate and nowhere else in the apparatus, this corresponds to each molecule occupying a space of $\sim 2.5 \times 10^{-22}$ – $2.5 \times 10^{-23} \text{ cm}^3$, or a region with a linear lengthscale of $L \sim 3 \times 10^{-8}$ – $6 \times 10^{-8} \text{ cm}$. The number of occupied sites in a monolayer (ML) per unit area is then $1/L^2 \sim 0.3$ – $1.3 \times 10^{15} \text{ cm}^{-2}$. Here, we will take $N_s = 10^{15} \text{ cm}^{-2} \text{ ML}^{-1}$, which is consistent with astrochemical studies that were earlier described (e.g., Hollenbach et al. 2009; Bergin 2011; Fayolle et al. 2011). Depositing a $2 \mu\text{m}$ thick layer of ice, means that there were ~ 3200 – 6900 monolayers of ice in the sample. Taking 5000 layers as typical, these estimates give a total number of deposited molecules in the experiments of: $10^{15} \text{ molecules cm}^{-2} \text{ layer}^{-1} \times 5000 \text{ layers} \times 12.5 \text{ cm}^2 = 6.25 \times 10^{19}$ molecules, which is in line with the estimates reported by Bar-Nun et al. (1987). In this paper, we focus on a particular unit area (1 cm^2) suspended so that the number of

surface sites available is $N_s = 10^{15}$ species per layer and that the volume density of particles is $n_d = 1 \text{ cm}^{-3}$.

Given these estimates, the flux of molecules onto the plate can be estimated. The fluence needed to build a $1 \mu\text{m}$ thick layer of ice is $2500 \text{ ML} \times 10^{15} \text{ sites cm}^{-2} \text{ ML}^{-1} = 2.5 \times 10^{18} \text{ molecules cm}^{-2}$. The deposition rates used in these experiments ranged from $\text{DR} = 10^{-5} - 10^{-1} \mu\text{m minute}^{-1}$, which would require adsorption fluxes of:

$$F_{\text{dep}} = 4.2 \times 10^{15} \left(\frac{\text{DR}}{0.1 \mu\text{m minute}^{-1}} \right) \text{ species cm}^{-2} \text{ s}^{-1}. \quad (9)$$

This can be equated to the flux expected for gaseous species, $F_i \sim \frac{1}{4} n_i v_{\text{th},i}$. Thus, for a given temperature, we set the adsorption rate to the flux defined by the experimental deposition rate, with total H_2O and Ar fluxes summing to F_{dep} . These are set as inputs into our model, with the gaseous number densities and temperatures held constant throughout the period of deposition (that is, as species freeze-out, we assume that they are replaced through the experimental apparatus to keep the flux constant) as gas was constantly replenished by the steady flow over the plate in the experiments. Given these inputs, we calculate the build-up of the ice layers, tracking adsorption and desorption of the different species. Diffusion during this time is ignored because it is expected to be minor compared to the other processes during deposition. After deposition, the deposited sample was warmed and any gas that came off was pumped out of the experimental chamber at a constant rate. To simulate this, we increase the temperature of the solids by 1 K per minute, with all desorbed species being removed (gas phase abundance set to zero) to simulate the pumping of the chamber.

To demonstrate how the model predicts the behavior of such a mixed ice during warming and reproduces the physical effects seen in experiments, Figure 2 shows the results of a calculation for a $\text{H}_2\text{O}-\text{CO}_2$ mixture of gas, at a 5:1 ratio, that was deposited at a temperature of 10 K. This scenario was investigated experimentally and theoretically by Fayolle et al. (2011). Only a thin layer of ice formed in the experiments, approximately 20 ML. The best fit parameters for the three-phase model were found to be: $E_{\text{CO}_2} = 2440 \text{ K}$, and $c_{\text{CO}_2} = 20.5 \text{ ML}$. The release of CO_2 at around 80 K is due to the relatively high binding energy of the molecule to H_2O , which is the equivalent of the release of frozen, untrapped, gases in the experiments by Notesco et al. (2003). The results presented here match well those presented in Fayolle et al. (2011).

The relation of the swapping energy to the binding energy for CO_2 was slightly different in Fayolle et al. (2011), resulting in $E_{\text{diff}} = 1520 \text{ K}$, or $E_{\text{diff}}/E_{\text{CO}_2} \sim 0.6$, instead of 0.5 as assumed here. However, in that study, the authors found that the modeling results were relatively insensitive to the value of E_{diff} , with values ranging from 0.25 to $0.9E_{\text{CO}_2}$ matching the experimental results equally well. Instead, the availability coefficient, c_{CO_2} , had a stronger control on the amount of the volatile that was trapped versus that which could be freely released via desorption. We also find that our results do not vary significantly if we assume a different ratio of $E_{\text{diff}}/E_{\text{CO}_2}$, suggesting that our results will remain robust even if the relationship between these energies is more complicated than assumed here.

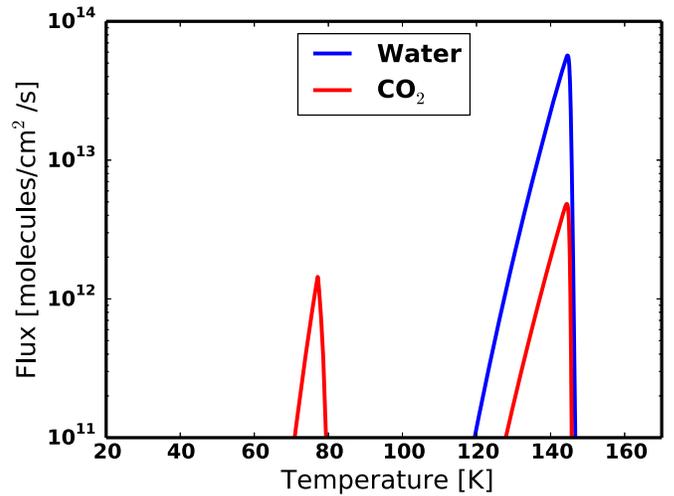


Figure 2. The flux of CO_2 and H_2O coming off of the ice as it is warmed in the calculations reproducing those of Fayolle et al. (2011). The peak at $\sim 80 \text{ K}$ arises from frozen CO_2 that desorbs directly from the surface of the ice, either as it was located there after deposition or because it diffused to there from the mantle. As water begins to desorb from the ice at $\sim 120 \text{ K}$, frozen CO_2 is also found to come off the ice. This CO_2 is assumed to have been trapped within the ice.

Turning back to Ar, we applied our model to simulate the experiments reported in Notesco et al. (2003) for $T = 22 \text{ K}$ and 27 K .³ A smaller number of experiments were also performed at 50 K , although these experiments did not see any frozen Ar being present, which makes them less useful in our full parameter space search here. We return to experiments at these higher temperatures later in our discussion. In all cases, the gas was assumed to exist above the cold plate at the temperatures of the experiment and at abundances such that the deposition fluxes summed to the value given by Equation (7), with $F_{\text{H}_2\text{O}} = F_{\text{Ar}}$, because the gas was meant to have a 1:1 mixture of the two species. Given that the gas was flowed across the cold plate, we assumed that these conditions remained fixed throughout the deposition period. The experiments yielded ice layers which were $\sim 0.1 \mu\text{m}$ thick, thus the time of deposition was set by $t_{\text{dep}} = 0.1/\text{DR}$ (ranging from 1 minute to 1 week). In each case, we varied the binding energy and availability coefficient, E_{Ar} and c_{Ar} , to compare our model's predictions to the experimental results. While the amount of trapped Ar is calculated for a given availability coefficient using Equation (7), the earliest stages of heating were simulated to ensure that all frozen Ar was desorbed before the temperatures increased much above the 40 K limit found in the experiments.

Figure 3 shows the results of a suite of model runs for deposition rates of $\text{DR} = 10^{-1}$ and $1.8 \times 10^{-5} \mu\text{m minute}^{-1}$ at a temperature of 27 K , two sets of experimental conditions reported by Notesco et al. (2003). In these final experiments, trapped Ar/ H_2O ratios of 0.1 and 0.03 were found within the ice, respectively. The trapped Ar/ H_2O ratios in the models are shown by the contours throughout the parameter space (varying E_{Ar} and c_{Ar}) that was explored.

We see two regimes of behavior in the cases explored in Figure 3. In the rapid deposition case, the final Ar/ H_2O ratio of

³ The deposition rates and Ar/ H_2O ratios were taken from the plots in that paper using datathief: <http://datathief.org>.

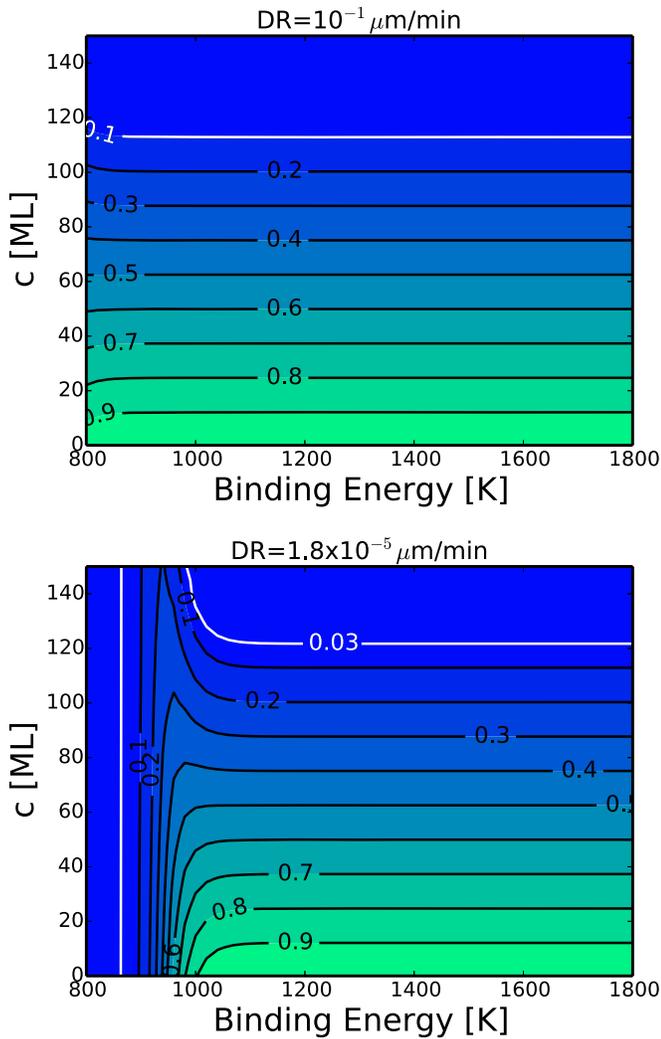


Figure 3. Contour maps showing the ratio of Ar/H₂O remaining in the ice after heating for deposition temperatures of $T = 27$ K model calculations, with deposition rates of 10^{-1} (top) and 1.8×10^{-5} (bottom) $\mu\text{m minute}^{-1}$, for various values of assumed Ar binding energy and availability for diffusion. White contours indicate the value of Ar/H₂O found in the experiments.

the ice is independent of the binding energy, E_{Ar} , and is purely set by the availability constant c_{Ar} . Given that the availability constant sets the amount of Ar that is trapped in the ice for a given mixing fraction after deposition (x_{Ar}), the mixing fraction after deposition in this case was nearly the same for all of the binding energies considered here.

In the slow deposition case, we see a regime, at low binding energies, where the amount of trapped Ar is set purely by the binding energy and is nearly independent of the availability constant. In these cases, we see very small values for the trapped Ar abundance (trapped Ar/H₂O in the ice < 0.2). These binding energies (< 1000 K) yield a short residence time for Ar on the ice. Therefore, a water molecule has a small, finite amount of time to cover the Ar before the Ar is desorbed. This results in only a tiny number of Ar atoms being incorporated as the ice thickens. Due to the low concentration of Ar (x_{Ar}) that remains in the ice, a very high amount is trapped, which leaves negligible amounts to migrate and be lost during initial heating.

For the cases illustrated here, binding energies above ~ 1000 K are high enough so that at 27 K essentially all of

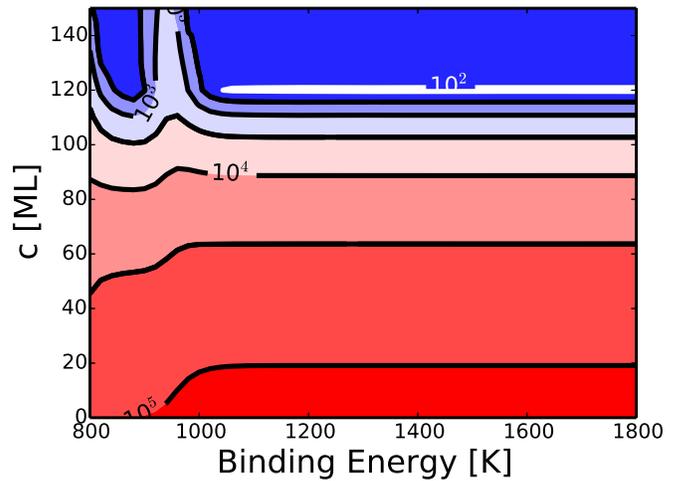


Figure 4. Contours for the sum of squares of the weighted residuals, χ^2 , in the parameter space for the $T = 22$ K and $T = 27$ K experimental results. Similar structure in contour plots are seen as in Figure 3 as a result of the processes described in the text. The lowest values (best fit) are for $E_{\text{Ar}} \sim 1000$ – 1600 K and $c_{\text{Ar}} = 120$ ML.

the adsorbed Ar atoms remain on the surface long enough during deposition to be buried and incorporated into the mantle. There is slight variation on the minimum binding energy where this occurs for the different deposition rates. The cases with higher deposition rates allow Ar to be buried more readily as the timescale for forming monolayers (and burying adsorbed species) is lower, thus the residence time of Ar need not be as long.

Figure 4 shows the sum of the squares of the weighted residuals for our parameter exploration:

$$\chi^2 = \sum \left(\frac{r_i^m - r_i^e}{\sigma_i^e} \right)^2 \quad (10)$$

where r_i^m is the model prediction for the trapped Ar/H₂O ratio, r_i^e is the experimentally determined ratio, and σ_i^e is the uncertainty on the measured rate, which we take as 20% of the experimental value as these were the variations seen in experiments when a experimental conditions were repeated (Notesco & Bar-Nun 2005). Here, we have simply applied the model fit to the $T = 22$ K and $T = 27$ K runs. In the $T = 50$ K case, there is no frozen Ar and, therefore, those cases provide little constraint on c_{Ar} . Furthermore, given the experimental chamber described above, these cases could have the greatest temperature gradients, leading to greater uncertainty in the results.

The fits indicate that the experimental results are reproduced well by $E_{\text{Ar}} > 1000$ and $c_{\text{Ar}} = 120$ ML. These constraints are consistent with similar efforts by Fayolle et al. (2011), who also found that a wide range of binding energies were able to reproduce the experimental results for CO₂ and CO, while only a small range of availability constants gave satisfactory fits. Given these results, we take our best fit parameters to be $E_{\text{Ar}} = 1010$ K and $c_{\text{Ar}} = 120$ ML. While this energy is on the low end of the well-fit range, the higher energies can be ruled out as they would lead to frozen Ar being released at temperatures much greater than 40 K, inconsistent with the experimental results. Further, if the trapped Ar abundances reported in the experiments represent an upper limit in terms of

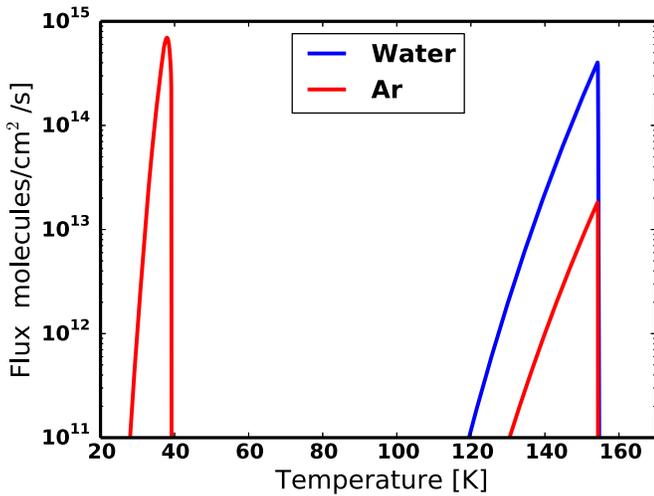


Figure 5. Similar to Figure 2, but for Ar and H₂O release. Frozen Ar is released around ~ 40 K, while the trapped Ar is released concurrently with the water vapor, which is in agreement with Notesco & Bar-Nun (2005). Note that the instantaneous flux is plotted here as a function of temperature. While the water flux does not reach the same height as the Ar plot at lower temperatures, the integrated fluxes indicate that an equal amount of Ar and H₂O were present when warming began.

Ar/H₂O ratios in the ice, then the fitted values for the binding energy would also represent an upper limit on this parameter, favoring a lower binding energy. We further justify this choice of the binding energy below when considering the experimental results of Yokochi et al. (2012).

Figure 5 shows the calculated release of vapor in one of our models for a deposition temperature of 27 K and deposition rate of $10^{-3} \mu\text{m minute}^{-1}$ using our best fit parameters. The general behavior shown here is the same as in the CO₂ release illustrated Figure 2 and in good agreement with the experiments described by Notesco et al. (2003). That is, frozen Ar is released up to temperatures around $T \sim 40$ K, and then all other Ar remains within the solid until water begins to vaporize at $T > 120$ K. This shows that the binding energy used here is appropriate, as higher values would have led the frozen Ar desorb at too high of a temperature, while lower values would have had it desorb when it was too cool. Further, when models are run with deposition temperatures of 50 K, no frozen Ar is seen, again in agreement with the experiments of Notesco et al. (2003).

5. Extrapolation to Astrophysical Conditions

To date, experimental studies have generally been done at deposition rates of $10^{-3} \mu\text{m minute}^{-1}$ or higher. At 20 K, this would correspond to a water vapor density of $n_{\text{H}_2\text{O}} \sim 10^{10} \text{ cm}^{-3}$. Water is typically present in a gas of solar composition with a ratio of $n_{\text{H}_2\text{O}}/n_{\text{H}_2} = 5 \times 10^{-4}$ (Lodders 2003; Cleeves et al. 2014), meaning the experimental fluxes correspond to environments with n_{H_2} of $2 \times 10^{13} \text{ cm}^{-3}$ or higher. These densities are generally expected toward the inner regions (< 5 au) of a protoplanetary disk (densities of $\sim 10^{-10} \text{ g cm}^{-3}$ or pressures of $\sim 5 \times 10^{-8}$ bars, e.g., Ciesla & Dullemond 2010; Bergin 2011). However, amorphous ice is much more likely to form in the very outer regions of the solar nebula, possibly above the disk midplane, or in the natal molecular cloud from which the solar system formed (Kouchi et al. 1994; Ciesla 2014). In these cases, hydrogen number densities were probably much less, possibly as low as $n_{\text{H}_2} = 10^3\text{--}10^{10} \text{ cm}^{-3}$ (Bergin 2011), which implies that

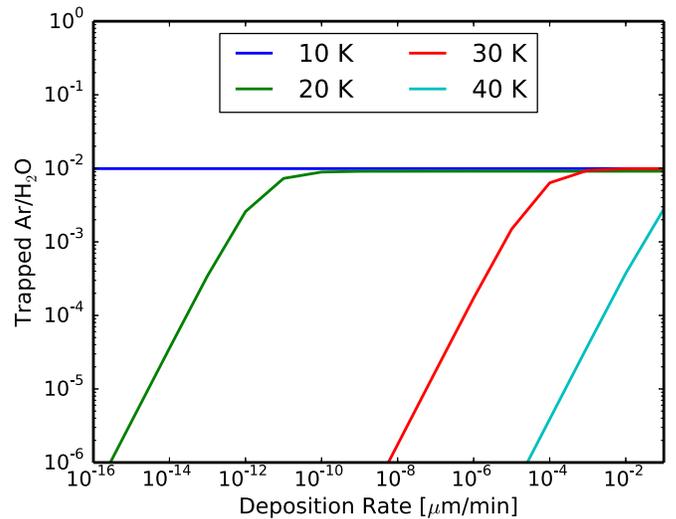


Figure 6. The predicted trapped Ar/H₂O ratio of ices formed in a gas of solar composition at various temperatures and deposition rates. The *Burial Regime* is reached when the Ar/H₂O ratio in the ice mirrors that of the gas and is independent of deposition rate. The *Equilibrium Regime* is reached when the abundance of Ar is a function of deposition rate. The transition between these regimes occurs approximately where the timescale for desorption of an Ar atom is comparable to the timescale for a monolayer of water ice to form over that Ar atom.

the deposition fluxes were as much as 10–12 orders of magnitude lower than those used in experiments.

Taking the best fit parameters from above, we can apply the three-phase model to examine how much Ar would be trapped at the much lower deposition rates expected in these astrophysical environments. We assume a gas of solar composition ($\text{Ar}/\text{H}_2 = 5 \times 10^{-6}$ Asplund et al. 2009), which gives gas phase ratios $\text{Ar}/\text{H}_2\text{O} = 0.01$, assuming that all of the water is initially present as a vapor. We consider temperatures of 10, 20, 30, and 40 K and deposition rates ranging from the $10^{-1} \mu\text{m minute}^{-1}$ used in the experiments, down to $10^{-16} \mu\text{m minute}^{-1}$. The extremely slow deposition rates would obviously require time periods longer than the age of the universe to produce ice layers of the thicknesses modeled here. However, these are not meant to be realistic scenarios but rather show how the trapping behavior, even at low temperatures, varies with deposition flux to develop an intuitive understanding of the key parameters. In all cases, the same approach was followed as before: ice was deposited to form a layer measuring $0.1 \mu\text{m}$ thick at constant deposition rates and temperatures, with all gases replenished as in the experiments. While this would not be the case in reality if a particle stayed dynamically bound to the same gas in a given environment, this was done to make the comparisons to the experiments easier (we will later return to this issue).

Figure 6 shows the results of these calculations, where two regimes of trapping are readily seen. The first is a *burial regime*, where the Ar/H₂O ratio of the ice is roughly comparable to that of the gas (~ 0.01). This is seen at low temperatures and high deposition rates. The second is a *equilibrium regime*, where the trapped Ar/H₂O ratio is proportional to the deposition rate. This is seen at higher temperatures and low deposition rates. The transition between the two trapping regimes represents a shift in the likelihood of an adsorbed Ar atom being trapped by water molecules during deposition. This shift occurs when the timescale for a monolayer of water to be deposited becomes comparable to, or exceeds, the residence time for an Ar atom on the surface of

the ice. That is, the typical amount of time that an Ar atom would spend on the surface after adsorption would be $t_{\text{res}} = \nu_{\text{Ar}}^{-1} \exp\left(\frac{E_{\text{Ar}}}{T}\right)$, while the timescale for a monolayer of water ice to form is $t_{\text{ML}} = N_s/F_{\text{H}_2\text{O}}$. In all cases, Ar is continuously adsorbed onto the surface of the ice. For cases when $t_{\text{res}} > t_{\text{ML}}$, the Ar atoms sit on the surface long enough to be covered by layers of water ice, meaning that their abundance is set only by how quickly they are delivered to the ice. When $t_{\text{res}} < t_{\text{ML}}$, the Ar atoms are relatively transient and, therefore, many are able to desorb before being covered with water. This allows the total amount of Ar on the surface to be set by the relative rates of adsorption and desorption, resulting in some equilibrium coverage for this species.

This equilibrium trapping was observed in experiments by Yokochi et al. (2012), where the amount of Ar that was trapped in amorphous water ice varied with the pressure of Ar during ice deposition. These authors proposed that the pressure dependence seen in their experiments (Ar/H₂O ratio was proportional to the partial pressure of Ar in the experiments) was due to this equilibrium effect, where the amount of Ar on the ice was able to rapidly adjust before being buried by a layer of trapping water. Because these experiments were performed at ~ 77 K, the high temperatures would imply very short residence times of any guest species, putting them squarely in the equilibrium regime. Within the framework that is given here, the equilibrium abundance of Ar on the surface of the grain would be set by setting the desorption and adsorption fluxes onto the substrate (Bergin 2011):

$$\frac{1}{4} n_{\text{Ar}}^g \nu_{\text{th}}^{\text{Ar}} = n_{\text{Ar}}^s \nu \exp\left(-\frac{E_{\text{Ar}}}{T}\right). \quad (11)$$

Writing n_{Ar}^g as P_{Ar}/kT , we see that the abundances of Ar on the surface will be proportional to the partial pressure of Ar. Following this, we can write the Ar/H₂O ratio of the ice to be:

$$\frac{n_{\text{Ar}}^s}{n_{\text{H}_2\text{O}}^s} = \frac{\nu_{\text{th}}^{\text{Ar}}}{4kTn_{\text{H}_2\text{O}}^s} \nu^{-1} \exp\left(\frac{E_{\text{Ar}}}{T}\right) P_{\text{Ar}}. \quad (12)$$

Yokochi et al. (2012) found that the Ar/H₂O ratio in the ice was given by $2.34 \times 10^{-4} P_{\text{Ar}}$, if the pressure is given in μbars . Taking that value as the proportionality factor in Equation (11), and assuming that in the equilibrium stage that water dominates the surface ($n_{\text{H}_2\text{O}}^s \sim 10^{15} \text{ cm}^{-2}$) allows us to estimate $E_{\text{Ar}} = 1010$ K, which justifies our previous choice. We also modeled cases where the Ar/H₂O ratio in the gas was varied for those cases which were found to be in the *equilibrium* regime. We found that the final Ar/H₂O ratio in the ice was independent of this value in the gas provided $t_{\text{res}} < t_{\text{ML}}$, again in agreement with the experimental findings of Yokochi et al. (2012).⁴

Smith et al. (2016) also reported results from an experimental study of the desorption of Ar from amorphous ice. Their experiments were not focused on the trapping of Ar during ice deposition; rather, they deposited Ar at a temperature of 25 K on the surface of already formed amorphous ice and

then examined when Ar desorbed off of the surface upon heating. They found that the desorption relationship followed a similar formula as that used here (Equation 2), but with a pre-exponential factor of $\nu = 6.2 \times 10^{11} \text{ s}^{-1}$ and $E_{\text{Ar}} = 870$ K. Using these values and following the previous arguments, would lead to a predicted transition between equilibrium and burial trapping at higher deposition rates for the temperatures of interest considered here. Specifically, the residence times using the Smith et al. (2016) numbers would be shorter by a factor of ~ 20 at 40 K, and ~ 700 at 20 K. At 77 K, the residence time predicting is changes by a factor of just ~ 4 , leaving the Yokochi et al. (2012) experiments still squarely in the Equilibrium regime.

Diffusion only plays a minor role in the trapping of Ar in these cases. This is due to the relatively low abundance of Ar in the deposited ice ($x_{\text{Ar}}^{\text{ini}} \leq 0.01$), which according to Equation (6), means that most ($>99\%$) of the Ar in the mantle is prevented from exchanging with the surface. Diffusion would only become important in cases where Ar/H₂O ratios were much higher than in a gas of solar composition. This is true even for different values of β in Equation (6) and is consistent with experimental results, which suggests that the importance of diffusion decreases for high ratios of water to the trapped volatile.

The model used here necessarily simplifies some of the processes that are likely at work when amorphous water ice forms and traps guest species. For example, it was assumed that the structure of the water ice was independent of the formation temperature. Notesco et al. (2003) discussed how the surface area of water varies depending on the conditions at which it is deposited. This is probably related to the ability of water molecules to arrange in the binding sites available in the layers provided by a given surface, and as such the morphology of the ice likely varies with the temperature of formation. This is important because nanopores in the ice may provide sites where adsorbed gases may be more strongly adsorbed (i.e., have a higher binding energy) than other sites in the ice. This effect has previously been noted for CO in amorphous water ice (Karssemeijer et al. 2014). Smith et al. (2016) also discussed how, given the structure of amorphous ice, there exists a distribution of binding site energies, with the derived values describing desorption representing the most probable value in that distribution. Therefore, the binding energies are not likely to be constant, and the available surface area and density of surface sites may vary with deposition temperature. These effects should be looked at to better understand the trapping ability of ices that form at very cold environments. Visser et al. (2009) considered a distribution of binding energies for CO while investigating its retention during molecular cloud collapse and protoplanetary disk formation, and documenting this distribution in detail for various species will be important.

We assumed that the deposition flux was constant throughout deposition. Meanwhile, in real astrophysical environments, the gas phase abundance would decrease as species adsorbed onto solids, leading to changes in deposition rates with time. Because water molecules have a lower mass than Ar atoms, the rate of depletion of water vapor would be faster. This means that the Ar composition would not be uniform in the mantle and the Ar/H₂O ratio would increase as it moved closer to the surface. This could mean that greater fractions of Ar would be lost via desorption during warm up because migration would be more important in regions of higher Ar/H₂O ratios,

⁴ As discussed by Yokochi et al. (2012), their experiments generally found lower trapping efficiency than those in Bar-Nun et al. (1988). This may be due to different experimental approaches because Yokochi et al. (2012) considered trapping in a closed system, such that Ar could only freeze-out with water. As discussed previously, the numbers from the earlier experiments should be considered upper limits on the trapping efficiency rather than absolute values, which suggests that the two results may be in agreement with one another.

although this issue should be quantitatively examined by future experiments.

While the model that we have used here was simplified, it has successfully reproduced many of the features and relations observed in amorphous ice trapping experiments. Thus, this framework is useful to understand how species may be trapped in amorphous ice. Future experimental studies should be interpreted in this context, with the three-phase model allowing extrapolation from the laboratory conditions to astrophysical environments.

6. Summary and Discussion

Here we have applied the three-phase model to determine which parameters allow us to reproduce the experimental trapping results of Notesco et al. (2003) and we have applied that model to conditions that are more similar to those expected during the stages of planet formation. We have identified two different trapping regimes: *burial*, where the composition of the ice reflects the composition of the gas during deposition; and *equilibrium*, where the amount of trapped species scales with the density of the gas being trapped. Both regimes have been identified in experimental studies. Here we have developed a model to identify under what conditions each would occur. Burial trapping occurs under conditions that allow for rapid ice deposition and can be found when temperatures are very low, which allows gases to reside on the surface for long enough to be covered by another layer of deposited ice. Equilibrium trapping occurs when temperatures are higher or the rate of ice deposition is slow, which allows for the amount of Ar on the surface to be set by both adsorption and desorption.

If trapping of noble gases in amorphous ice is necessary to explaining the features that we see in planetary atmospheres and small bodies, then the results described here can help to constrain the formation conditions for these ices. Forming solar-composition solids that include noble gases as envisioned by Owen et al. (1999), requires conditions that result in burial trapping. For temperatures of 10, 20, 30, and 40 K, the transition between the burial and equilibrium trapping (when $t_{\text{res}} = t_{\text{ML}}$) occurs at deposition rates of $\sim 3 \times 10^{-34}$, 3×10^{-12} , 6×10^{-5} , and $0.3 \mu\text{m minute}^{-1}$, respectively (approximately where the transition from sloped to horizontal line occurs for the curves in Figure 6). These deposition rates correspond to environments with hydrogen densities of $n_{\text{H}_2} \sim 10^{-18}$, 10^4 , 10^{11} , and 10^{15} cm^{-3} respectively, assuming that all of the water is present as a vapor at a mixing ratio of $\text{H}_2\text{O}/\text{H}_2 = 5 \times 10^{-4}$. That is, burial trapping would occur in environments that are more dense than these critical values for the respective temperatures. At 10 and 20 K, the critical values are generally so low that molecular cloud or protoplanetary disk environments exceed them, implying that burial trapping would occur at these temperatures.

In the discussion thus far, we have assumed that water is present in the vapor when deposition occurs. This is generally not expected for the low temperatures where trapping is likely to occur (e.g., Fray & Schmitt 2009). As shown here, water will largely exist as a solid at temperatures < 100 K and is expected to be frozen out at these temperatures even at the pressures found in the interstellar medium (Sandford & Allamandola 1990; Fraser et al. 2001). Consequently, providing the water that will trap the noble gases at these temperatures requires some event or exterior input of energy that would lead to water molecules being liberated and then freezing-out at the fluxes

defined earlier. If some heating event were to occur (e.g., shock wave, impact plume) that vaporized the water, then the cooling timescale would have to be faster than the water freeze-out timescale for enough water to be present to then freeze-out at the relevant temperatures. The timescale for freeze-out of water is (Bergin 2011):

$$t_{\text{fo}} = 2 \times 10^4 \left(\frac{5 \times 10^4 \text{ cm}^{-3}}{n_{\text{H}_2}} \right) \left(\frac{20 \text{ K}}{T} \right) \text{ years} \quad (13)$$

assuming that the solids would be present at ISM abundances and sizes. Grain growth or depletion of solids would increase the freeze-out timescales, although they may also limit how much water is vaporized. The inverse dependence of the freeze-out timescale on gas density favors low-density environments for trapping (as it would make it easier to satisfy $t_{\text{cool}} < t_{\text{fo}}$).

An alternative method by which water may be liberated into the vapor at these low temperatures is through photodesorption, where UV photons provide the energy for molecules to be lost from the surface (Westley et al. 1995; Öberg et al. 2009b). This effect is believed to be responsible for the cold water vapor that is seen in the outer regions of disks such as TW Hydra (Hogerheijde et al. 2011). Ciesla (2014) showed that the movement of grains into the surface regions of the disk via turbulent diffusion could expose them to sufficient UV to lose most, if not all of the water on their surfaces, only to have the water freeze-out at very high fluxes as the gas and then vapor diffuse toward the midplane again. The corresponding fluxes of water during freeze-out would have been $\sim 10^5$ – 10^9 molecules $\text{cm}^{-2} \text{ s}^{-1}$. This yields t_{ML} of 10^6 – 10^{10} s, which suggests that burial trapping can occur provided that temperatures are < 25 K (when $t_{\text{res}} > t_{\text{ML}}$).

Monga & Desch (2015) also invoked photodesorbed water as a means of producing amorphous ice and trapping noble gases to eventually enhance the abundance in Jupiter. In that study, the solids had grown and settled to the midplane, reducing the available surface area on which water molecules could freeze-out. As a result, water molecules would diffuse downward and outward from where they were photodesorbed for timescales of $\sim 10^3$ years or longer, resulting in $\sim 0.1 M_{\oplus}$ of water vapor in an annulus ranging from 30 to 50 au. Assuming that the gas is uniformly distributed over a height of 2 scale-heights (one on each side of the disk midplane with $H \sim 0.05r$), this would imply a water volume density of $n_{\text{H}_2\text{O}} \sim 10^5 \text{ cm}^{-3}$, suggesting a freeze-out flux of 10^9 molecules $\text{cm}^{-2} \text{ s}^{-1}$. Again, this would mean that burial trapping will occur in those regions only where temperatures < 25 K.

These two scenarios only consider UV photodesorption as a source of cold water vapor. Sputtering by cosmic rays can also liberate water from ices (e.g., Dartois et al. 2015), though the importance of this effect will depend on the cosmic ray flux. It is possible that stellar winds from the young Sun prevented significant penetration of cosmic rays into the solar nebula (Cleeves et al. 2013), which would limit this effect. However, if trapping occurs within dense molecular clouds, then this may be an important source of water vapor.

The exact amount of water that is available in the gas phase is also important in determining how much Ar will be trapped as amorphous ice forms. The discussions thus far have assumed that water is present at its solar abundance relative to Ar when trapping occurs. However, it is possible that only a portion of water will be removed in whatever process produces the cold water vapor, or that some fraction will freeze-out before

conditions reach those where noble gases can be effectively trapped. If only a portion of the water is available in the gas, then this would alter the ratio of Ar/H₂O in the vapor, and thus the resulting mix in the ices that are deposited on the surfaces of the grains. As discussed earlier, the solar ratio of Ar/H₂O \sim 0.01 means that low Ar concentration would lead to very large fractions, nearly all of it, being trapped in the water ice. If only \sim 1% of the water is liberated into the gas, then the Ar/H₂O ratio in the vapor would be 1:1, which is similar to the experiments that were carried out by Natesco et al. (2003) and Natesco & Bar-Nun (2005). In the context of the model presented here, this would increase the abundance of Ar in the outermost ice layers, increasing the likelihood of Ar diffusing and desorbing from the surface of the grains upon warming, reducing the efficiency of this process. However, experiments have also indicated that once a trapped species exceeds \sim 25%–30% of the H₂O abundance, then the H-bonding network is effectively disrupted and the trapped species can leave far more easily (Sandford & Allamandola 1988). Thus, burial trapping is unlikely under these conditions and it is much more likely to occur in environments or conditions where large amounts of water are vaporized. In the models of Ciesla (2014), large freeze-out fluxes tended to occur when large amounts of water were vaporized. These conditions are ideal for burial trapping but occur less frequently because they require movement to higher altitudes above the disk midplane. In Monga & Desch (2015), high Ar/H₂O abundances are expected at lower heliocentric distances, which reduce the fraction of Ar that is trapped instead of frozen. This suggests that efficient trapping would have to be limited to the very outer regions of the zone that they had envisioned.

Consequently, the best environments for trapping noble gases in amorphous ice will be those where temperatures are $<$ 25 K and water is liberated into the gas such that it is at least \sim 10 \times more abundant than those species. The very outer regions of protoplanetary disks and molecular clouds, where photodesorption or localized heating events occur, would be the best candidates. However, even if trapping does occur in these locations, what gets delivered to comets or planets will ultimately depend on what happens to the icy particle after trapping occurs. Within the solar nebula, individual grains are likely to see a wide range of physical environments once they have been added to the disk as part of the infall and early evolution (e.g., Visser et al. 2009) or as they are subjected to dynamic processes within the disk (Ciesla & Sandford 2012). When amorphous H₂O-rich ices are warmed, they can go through several intermediate phase changes before the H₂O sublimates, this includes: (i) a change between two different amorphous states, (ii) a transition from amorphous ice to cubic crystalline ice (at 120 K), and (iii) just as the ice is subliming, a partial transition to hexagonal ice (at 150 K) (e.g., Bar-Nun et al. 1988; Sandford & Allamandola 1988; Blake et al. 1991). This can result in the expulsion of some trapped volatiles (Sandford & Allamandola 1988; Collings et al. 2003), although it is possible for some to be retained but in the form of clathrates instead of amorphous ice (Blake et al. 1991). Only a small amount of volatiles are lost at any given time (Viti et al. 2004). The details of transport and volatile retention will be the focus of our future work.

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References

- Asplund, M., Grevesse, N., Sauval, A. J., & Scott, P. 2009, *ARA&A*, **47**, 481
- Balsiger, H., Altwegg, K., Bar-Nun, A., et al. 2015, *SciA*, **1**, 8
- Bar-Nun, A., Herman, G., Laufer, D., & Rappaport, M. L. 1985, *Icar*, **63**, 317
- Bar-Nun, A., Kleinfeld, I., & Kochavi, E. 1988, *PhRvB*, **38**, 7749
- Bar-Nun, A., Prialnik, D., Laufer, D., & Kochavi, E. 1987, *AdSpR*, **7**, 45
- Bergin, E. A. 2011, in *Physical Processes in Circumstellar Disks around Young Stars*, ed. P. J. V. Garcia (Chicago, IL: Univ. Chicago Press), 55
- Biham, O., Furman, I., Pirronello, V., & Vidali, G. 2001, *ApJ*, **553**, 595
- Blake, D., Allamandola, L., Sandford, S., Hudgins, D., & Freund, F. 1991, *Sci*, **254**, 548
- Chaabouni, H., Diana, S., Nguyen, T., & Dulieu, F. 2018, *A&A*, **612**, A47
- Ciesla, F. J. 2014, *ApJL*, **784**, L1
- Ciesla, F. J., & Dullemond, C. P. 2010, in *Protoplanetary Dust: Astrophysical and Cosmochemical Perspectives*, ed. D. A. Paai & D. S. Lauretta (Cambridge: Cambridge Univ. Press), 66
- Ciesla, F. J., & Sandford, S. A. 2012, *Sci*, **336**, 452
- Cleeves, L. I., Adams, F. C., & Bergin, E. A. 2013, *ApJ*, **772**, 5
- Cleeves, L. I., Bergin, E. A., Alexander, C. M. O., et al. 2014, *Sci*, **345**, 1590
- Collings, M. P., Dever, J. W., Fraser, H. J., & McCoustra, M. R. S. 2003, *Ap&SS*, **285**, 633
- Dartois, E., Augé, B., Boduch, P., et al. 2015, *A&A*, **576**, A125
- Dauphas, N. 2003, *Icar*, **165**, 326
- Fayolle, E. C., Öberg, K. I., Cuppen, H. M., Visser, R., & Linnartz, H. 2011, *A&A*, **529**, A74
- Fraser, H. J., Collings, M. P., McCoustra, M. R. S., & Williams, D. A. 2001, *MNRAS*, **327**, 1165
- Fray, N., & Schmitt, B. 2009, *P&SS*, **57**, 2053
- Garrod, R. T. 2013, *ApJ*, **765**, 60
- Gautier, D., Hersant, F., Mousis, O., & Lunine, J. I. 2001, *ApJL*, **550**, L227
- Hasegawa, T. I., & Herbst, E. 1993, *MNRAS*, **263**, 589
- Hogerheijde, M. R., Bergin, E. A., Brinch, C., et al. 2011, *Sci*, **334**, 338
- Hollenbach, D., Kaufman, M. J., Bergin, E. A., & Melnick, G. J. 2009, *ApJ*, **690**, 1497
- Karssemeijer, L. J., Ioppolo, S., van Hemert, M. C., et al. 2014, *ApJ*, **781**, 16
- Kouchi, A., Yamamoto, T., Kozasa, T., Kuroda, T., & Greenberg, J. M. 1994, *A&A*, **290**, 1009
- Lodders, K. 2003, *ApJ*, **591**, 1220
- Lunine, J. I., & Stevenson, D. J. 1985, *ApJS*, **58**, 493
- Marty, B., Altwegg, K., Balsiger, H., et al. 2017, *Sci*, **356**, 1069
- Monga, N., & Desch, S. 2015, *ApJ*, **798**, 9
- Mousis, O., Lunine, J. I., Luspay-Kuti, A., et al. 2016, *ApJL*, **819**, L33
- Natesco, G., & Bar-Nun, A. 2005, *Icar*, **175**, 546
- Natesco, G., Bar-Nun, A., & Owen, T. 2003, *Icar*, **162**, 183
- Natesco, G., Laufer, D., Bar-Nun, A., & Owen, T. 1999, *Icar*, **142**, 298

- Öberg, K. I., Fayolle, E. C., Cuppen, H. M., van Dishoeck, E. F., & Linnartz, H. 2009a, *A&A*, **505**, 183
- Öberg, K. I., Linnartz, H., Visser, R., & van Dishoeck, E. F. 2009b, *Apl*, **693**, 1209
- Owen, T., Mahaffy, P., Niemann, H. B., et al. 1999, *Natur*, **402**, 269
- Sandford, S. A., & Allamandola, L. J. 1988, *Icar*, **76**, 201
- Sandford, S. A., & Allamandola, L. J. 1990, *Icar*, **87**, 188
- Smith, R. S., May, R. A., & Kay, B. D. 2016, *JPCB*, **120**, 1979
- Visser, R., van Dishoeck, E. F., Doty, S. D., & Dullemond, C. P. 2009, *A&A*, **495**, 881
- Viti, S., Collings, M. P., Dever, J. W., McCoustra, M. R. S., & Williams, D. A. 2004, *MNRAS*, **354**, 1141
- Westley, M. S., Baragiola, R. A., Johnson, R. E., & Baratta, G. A. 1995, *P&SS*, **43**, 1311
- Yokochi, R., Marboeuf, U., Quirico, E., & Schmitt, B. 2012, *Icar*, **218**, 760